

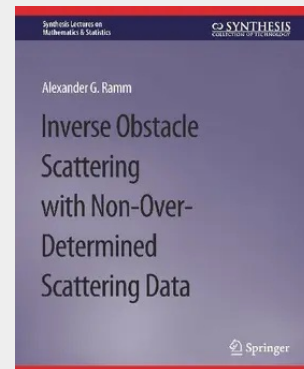
Inverse Obstacle Scattering with Non-Over-Determined Scattering Data

The inverse obstacle scattering problem consists of finding the unknown surface of a body (obstacle) from the scattering $g(\theta, \theta_0; k)$, where $g(\theta, \theta_0; k)$ is the scattering amplitude, $\theta, \theta_0 \in \mathbb{R}^2$ is the direction of the scattered, incident wave, respectively, $\mathbb{S}^1$ is the unit sphere in the $\mathbb{R}^2$ and $k > 0$ is the modulus of the wave vector. The scattering data is called non-over-determined if its dimensionality is the same as the one of the unknown object. By the dimensionality one understands the minimal number of variables of a function describing the data or an object. In an inverse obstacle scattering problem this number is 2, and an example of non-over-determined data is $g(\theta, \theta_0; k) := g(\theta, \theta_0; k_0)$. By sub-index 0 a fixed value of a variable is denoted.

It is proved in this book that the data $g(\theta, \theta_0; k)$, known for all θ, θ_0 in an open subset of $\mathbb{S}^1 \times \mathbb{S}^1$, determines uniquely the surface Γ and the boundary condition on Γ . This condition can be the Dirichlet, or the Neumann, or the impedance type.

The above uniqueness theorem is of principal importance because the non-over-determined data are the minimal data determining uniquely the unknown Γ . There were no such results in the literature, therefore the need for this book arose. This book contains a self-contained proof of the existence and uniqueness of the scattering solution for rough surfaces.

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